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753

# Cepstral Domain Talker Stress Compensation for Robust Speech Recognition

Y. Chen

10 November 1986

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**Lincoln Laboratory**  
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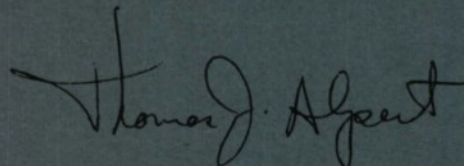
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FOR THE COMMANDER

A handwritten signature in dark ink, appearing to read "Thomas J. Alpert". The signature is fluid and cursive, with the first name "Thomas" and last name "Alpert" clearly distinguishable.

Thomas J. Alpert, Major, USAF  
Chief, ESD Lincoln Laboratory Project Office

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**CEPSTRAL DOMAIN TALKER STRESS COMPENSATION  
FOR ROBUST SPEECH RECOGNITION**

*Y. CHEN*

*Group 24*

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## **ABSTRACT**

Automatic speech recognition algorithms generally rely on the assumption that for the distance measure used, intraword variabilities are smaller than interword variabilities so that appropriate separation in the measurement space is possible. As evidenced by degradation of recognition performance, the validity of such an assumption decreases from simple tasks to complex tasks, from cooperative talkers to casual talkers, and from laboratory talking environments to practical talking environments.

This report presents a study of talker-stress-induced intraword variability, and an algorithm that compensates for the systematic changes observed. The study is based on Hidden Markov Models trained by speech tokens spoken in various talking styles. The talking styles include normal speech, fast speech, loud speech, soft speech, and talking with noise injected through earphones; the styles are designed to simulate speech produced under real stressful conditions.

Cepstral coefficients are used as the parameters in the Hidden Markov Models. The stress compensation algorithm compensates for the variations in the cepstral coefficients in a hypothesis-driven manner. The functional form of the compensation is shown to correspond to the equalization of spectral tilts.

Preliminary experiments indicate that a substantial reduction in recognition error rate can be achieved with relatively little increase in computation and storage requirements.

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# CEPSTRAL DOMAIN TALKER STRESS COMPENSATION FOR ROBUST SPEECH RECOGNITION

## 1. INTRODUCTION

Current speech recognition systems generally degrade significantly in performance if the systems are not both trained and tested under similar talking conditions. A major reason for performance degradation when testing and training conditions differ is that people speak differently under different conditions. Previous research has demonstrated that differences in speech patterns can be caused by psychological or emotional stress,<sup>1-5</sup> by the presence of intense background noise,<sup>5-7</sup> by a demanding perceptual-motor or mental task,<sup>2-4</sup> by physical exertion,<sup>2</sup> and by natural inconsistencies in pronunciation.<sup>8,9</sup> Despite the knowledge that speech patterns change in stress and in noise and the demonstration of degraded recognition performance in stress, little speech recognition research has been directed at modeling systematic changes observed and at developing recognition systems that are resistant to such changes.

This report presents a study of talker-stress-induced variations in speech cepstral coefficients, and an algorithm that compensates for systematic (but unknown *a priori*) changes observed. The study is based on an isolated-word Hidden Markov Model speech recognizer trained by speech spoken in various talking conditions. The organization of this report is as follows. In Section 2 a speech data base that has been used in the study is described. In Section 3 a baseline Hidden Markov Model (HMM) speech recognizer is defined. In Section 4 a multistyle training experiment is described. The success of the multistyle training experiment has prompted the study of the stress-induced changes in speech, which is discussed in Section 5, and the development of a stress compensation algorithm, which is discussed in Section 6. The compensation algorithm may be interpreted as an adaptive, word-hypothesis-driven form of spectral tilt equalization. Section 7 presents experimental results.

Except otherwise noted, the notations used in this report are as follows: boldfaced upper case letters such as "**A**" represent matrices, boldfaced lower case letters such as "**b**" represent column vectors, and lower case letters such as "**c**" represent scalars. Elements of matrices and vectors may be written as scalars with an appropriate number of subscripts. The lower case letters *i* and *j* are used as indices, the upper case letters *N* and *M* are used to indicate dimensionalities. Therefore, the matrix **A** may be written as  $[a_{ij}]_{MN}$ , the vector **b** may be written as  $[b_i]_N$ . Lower case letters followed by one or more arguments enclosed in parentheses, such as "**f(x)**," represent functions.

## 2. THE "SIMULATED STRESS" SPEECH DATA BASE

The studies and experiments conducted in this research were based on the "simulated stress"<sup>10</sup> speech data base recently collected by Texas Instruments, Inc.

In this data base stress-like degradations of the speech signal were elicited by asking the speaker to produce speech in a variety of styles (normal, fast, loud, soft, and shout) as well as

with 95-dB pink noise exposure in the ear to produce the Lombard effect.<sup>5</sup> The vocabulary consisted of 105 words, including monosyllabic, polysyllabic, and confusing words. A complete list of the words is given in the Appendix.

The data base was divided into training data and test data. Training data consisted of five samples of each of the 105 words collected in a random order under normal talking conditions, and test data consisted of two samples of each word under each simulated-stress condition. Data were collected from five adult males and three adult females using a 16-bit A/D converter, sampled at 20-kHz rate, in a quiet laboratory environment. The data were downsampled to 8 kHz for laboratory usage. The total number of test word tokens was 10,080.

To verify the effects of "simulated stress," a baseline Hidden Markov Model based recognizer (to be described in the next section) has been tested on this data base. Substitution rate (no rejection or deletion was allowed in the experiments) of this test is given in Table I. It is seen that, relative to normally spoken speech, the error rate increases significantly for the various style conditions. It is the purpose of this research to understand the causes for the performance degradation experienced, and to develop effective means to compensate for them.

<p style="text-align: center;"><b>TABLE I</b></p> <p style="text-align: center;"><b>Substitution Rate (Percent):</b></p> <p style="text-align: center;"><b>The "Simulated Stress" Data Base</b></p>								
<b>Condition</b>	<b>Norm</b>	<b>Fast</b>	<b>Loud</b>	<b>Noise</b>	<b>Soft</b>	<b>Shout</b>	<b>Avg5*</b>	<b>Avg6†</b>
Baseline HMM	1.0	6.1	29.1	19.6	13.5	86.4	13.9	25.9
<p>* Avg5 is the average error rate of all talking conditons except shout.</p> <p>† Avg6 is the average error rate of all talking conditions.</p>								

### 3. A HIDDEN MARKOV MODEL SPEECH RECOGNIZER

The theory of Hidden Markov Models and the application of HMM to automatic speech recognition can be found in a number of papers.<sup>11-16</sup>

Figure 1 shows the type of HMM we used in this research. The word model network is a linear sequence of nodes with no skip branches. The model is intended to be used on speech inputs consisting of one word with background (silence) at each end; the first and the last nodes are background nodes to provide a semi-open-endpoint recognizer.



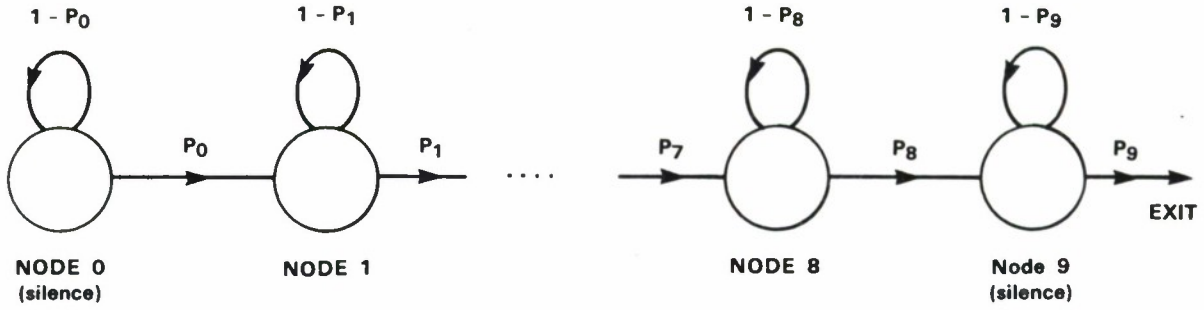


Figure 1. The 10-node left-to-right Markov model.

The HMM model can be described by a matrix-vector pair  $\{A, b\}$ .  $A = [a_{ij}]$  is a bidiagonal state transition matrix, its elements are given by

$$a_{ij} = \begin{cases} p_i & , & j = i + 1 & , \\ 1 - p_i & , & j = i & , \\ 0 & , & \text{otherwise} & . \end{cases} \quad (1)$$

Note that  $p_i$  is the transition probability from node  $i$  to node  $i + 1$ , and  $1 - p_i$  is the self-looping probability of node  $i$ . At each state a vector  $v$  of continuous variables is observed. The probabilistic nature of the vector  $v$  is described by a set of joint probability density functions  $b = [f_i(v)]$ .

The observation vector  $v$  contains 12 mel-frequency cepstral coefficients, i.e.,  $v = [v_j]_{12}$ . The cepstral coefficients are similar to those used by Davis and Mermelstein.<sup>17</sup> To compute a cepstral vector, 160 speech samples were read from the input, padded with 96 zeros, windowed by a 256-sample Hamming function and transformed into the frequency domain via 256-point FFT. In the frequency domain, magnitude of the spectrum is squared, multiplied by the function

$$g(f) = 1 + \frac{f^2}{250000} \quad , \quad (2)$$

where  $f$  is frequency in hertz, to boost high frequency content. Logarithms of the frequency samples are then taken. A set of 24 triangular-shaped windows (see Figure 2) are then used to compute averaged log spectral parameters  $x = [x_i]_{24}$ . Notice that the bandwidths of the windows increase as their center frequencies increase; the areas under the windows are kept constant.

From these averaged log spectral parameters  $x$  the cepstral coefficients  $v_j$  are computed as

$$v_j = \sum_{k=1}^{24} x_k \cos \left[ j \left( k - \frac{1}{2} \right) \frac{\pi}{24} \right] \quad j = 1, 2, \dots, 12 \quad (3)$$

Each node of the Hidden Markov Model is represented by a cepstral vector template which in turn is characterized by a jointly normal distribution with mean vector  $c$  and covariance

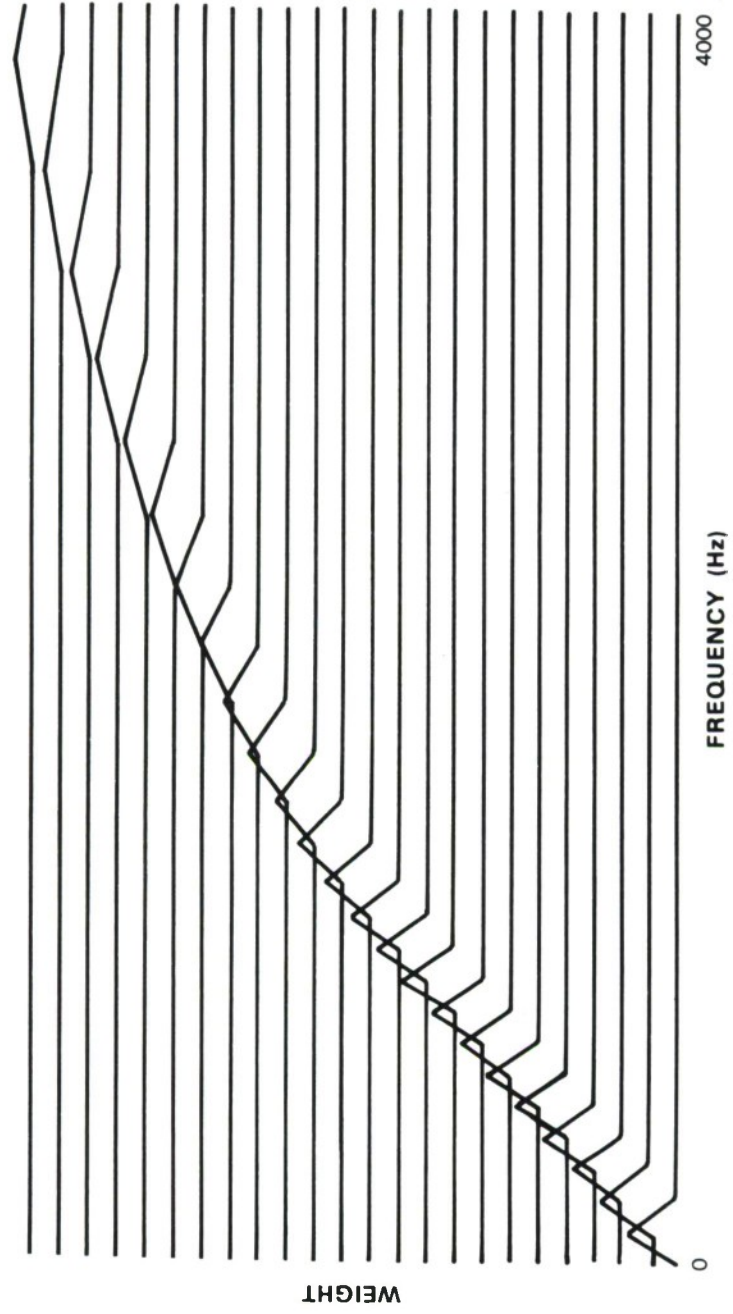


Figure 2. Filter bank used in Equation (1). (Courtesy of D.B. Paul.)

matrix  $\mathbf{R}$ . In our model, we assume that all off-diagonal elements of  $\mathbf{R}$  are zero. [This is justified in part by the fact that the result of the cosine transform in Equation (4) is approximately mutually uncorrelated.<sup>18,19</sup> Further justification is provided by the good recognition results obtained by us and by others using this assumption.] With this assumption, the covariance matrix can be reduced to a vector of variances, which we relabeled as  $\mathbf{r}$ .

In summary, the node transition characteristic of a Hidden Markov word model is described by the transition probability matrix  $\mathbf{A}$ ; the observation parameter statistics of each node are described by the cepstral mean vector  $\mathbf{c}$  and the cepstral variance vector  $\mathbf{r}$ .

Training of the models uses the forward-backward algorithm,<sup>20</sup> while recognition uses the Viterbi decoding algorithm.<sup>21</sup> Cepstral coefficients are computed once every 10 ms.

Since the recognizer makes a forced decision on each input word, substitution is the only type of error considered here.

#### **4. AN EXPERIMENT ON MULTISTYLE-TRAINED HIDDEN MARKOV WORD MODELS**

A number of different training/testing procedures could be used to improve speech recognition performance under stress. Ideally, a recognition system could be trained and tested under the same stress condition. This, however, is often not possible. A second alternative is to use dynamic adaptation of the models based on recent recognition results. This, again, may not be a satisfactory solution because stress conditions are transient. However, it is possible to use multistyle training.<sup>22</sup> Multistyle training requires a talker to train a recognizer using words spoken with different talking styles instead of using words all spoken normally. It has been found to be easy for a talker to change to styles such as fast, slow, loud, and soft, producing changes in speech characteristics that are similar to changes that occur under stress. It remains to be demonstrated that multistyle training produces improved recognition under stress.

An experiment on multistyle-trained Hidden Markov Model word recognition was performed. In this experiment, 11 speech tokens were used to train each word model: 5 tokens from the training data base, and 6 tokens, one per talking style except normal, from the test data base. Recognition tests were conducted on the remaining half of the test data base. The recognition error rates are listed in Table II. For comparison, the error rate of the baseline HMM system is also included.

In comparing experimental results listed in Table II, we see a dramatic improvement in recognition performance. It appears that the HMM word models were able to assimilate the data from the multiple styles and to capture statistically the more invariant features of each word. In the next section we investigate the gross changes of model parameters resulting from multistyle training as well as from style training (as opposed to normal training).



<p style="text-align: center;"><b>TABLE II</b></p> <p style="text-align: center;"><b>Substitution Rate (Percent): A Comparison of Normal- and Multistyle-Trained HMM Recognizers</b></p>								
Condition	Norm	Fast	Loud	Noise	Soft	Shout	Avg5	Avg6
Baseline HMM*	1.0	6.1	29.1	19.6	13.5	86.4	13.9	25.9
Multistyle†	0.5	5.6	5.1	2.1	5.8	43.6	3.8	10.5
<p>* The baseline system was trained with 5 normally spoken word tokens per talker and tested on 10,080 test tokens.</p> <p>† The multistyle-trained system was trained on 11 style speech tokens per talker and tested on 5,040 test tokens.</p>								

## 5. CEPSTRAL DOMAIN STRESS COMPENSATION — DRIVEN BY OBSERVATIONS

The success of the multistyle training experiment motivated a comparison of the model parameters trained under various talking styles to determine whether it would be possible to compensate for the cepstral changes through simple transformations on the cepstral means and variances obtained using normal training. Such transformation, if effective, would eliminate the need for asking the user to train the system with multiple styles and for incorporating multiple style data in the Forward-Backward training.

The differences among normally trained, single-style-trained, and multistyle-trained word models are partially reflected in the average shifts of the mean values and in the average scaling of the variances of the cepstral coefficients. To study such differences, seven different sets of word models were examined. Six of the models were trained under six individual conditions (normal training, fast, loud, Lombard, soft, and shout, respectively), while the seventh was trained using a composite of all these conditions (multistyle). The cepstral means and variances, averaged over all words in the TI vocabulary, over all speech nodes in each word, and over all talkers, were computed for each of the models above.

The mean cepstral shifts (i.e., cepstral means of the given model minus the cepstral means of the normal model) for each of the cepstral coefficients are tabulated in Table III(a). Figure 3(a) plots mean cepstral shifts for four cases: soft; shout; average of fast, loud, and Lombard; and multistyle. Figure 3(b) plots the corresponding spectra of these mean shifts, contrasting the effects on spectral tilt of low vocal effort (soft) vs higher vocal effort (fast, loud, Lombard, and shout). Increased vocal effort increases the relative high frequency content, whereas the opposite occurs with low vocal effort.

TABLE III							
Mean and Variance Variations in Style-Speech							
(a) Mean Shifts in Cepstral Domain*							
Coeff	Fast	Loud	Lomb	Soft	Shout	Multi	AVG
1	-0.61	-1.14	-0.84	0.90	-3.08	-0.61	-1.07
2	-0.26	-0.50	-0.59	0.43	-1.94	-0.43	-0.59
3	-0.03	-0.48	-0.34	0.37	-1.28	-0.26	-0.37
4	-0.06	-0.50	-0.36	0.49	-1.09	-0.25	-0.39
5	-0.02	-0.18	-0.08	0.27	-0.53	-0.10	-0.13
6	-0.02	-0.38	-0.29	0.27	-0.70	-0.17	-0.29
7	-0.02	-0.11	-0.05	0.12	-0.19	-0.03	-0.07
8	0.04	-0.18	-0.06	0.05	-0.40	-0.07	-0.09
9	-0.05	-0.16	-0.08	-0.01	-0.32	-0.06	-0.12
10	-0.06	-0.23	-0.10	-0.02	-0.53	-0.13	-0.17
11	-0.04	-0.13	-0.11	-0.03	-0.20	-0.10	-0.13
12	-0.06	-0.15	-0.15	0.04	-0.09	-0.05	-0.14
(b) Ratio of Variance							
Coeff		Multi		Coeff		Multi	
1		2.07		7		1.55	
2		1.84		8		1.70	
3		1.75		9		1.84	
4		1.71		10		1.77	
5		1.47		11		1.83	
6		1.62		12		2.10	

\* Because the differences in the fast, loud, and Lombard conditions are reasonably similar, their averages are listed in the last column.

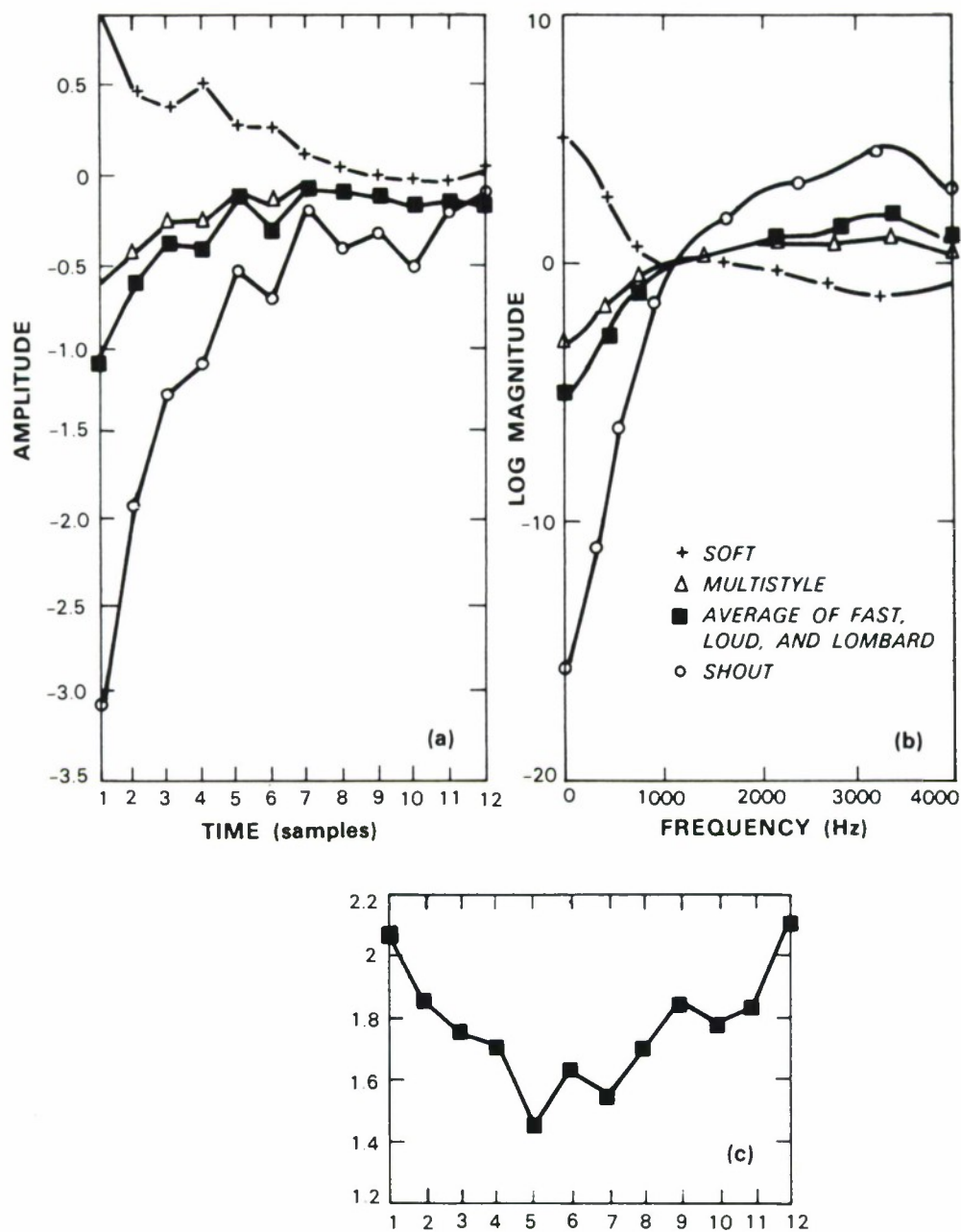


Figure 3. Variations of cepstral coefficient compared to normally spoken words. (a) Difference of mean (style minus normal), (b) spectra of differences of mean, and (c) ratio of variance (multistyle normal).



It is well known that spectral tilt exhibits large variation when a talker speaks under stress. Such variation usually contaminates the distance measure and is one of the most significant causes of recognition performance degradation. It appears that the effect of spectral tilt could be compensated, to some extent, by applying the appropriate cepstral compensation to normally trained word models.

Because variance estimation is less reliable than mean estimation, we have only compared cepstral variances of multistyle-trained models which used 11 training tokens with the normally trained models. Their ratios (multistyle/normal) are listed in Table III(b) and plotted in Figure 3(c). It appears that the major style-induced variations occur in the most slowly varying spectral components (corresponding to lower order cepstral coefficients), and in the most rapidly varying spectral components (corresponding to the higher order coefficients).

The following cepstral compensation experiments were performed, in which new word models were generated by modifying normally trained Hidden Markov word models by one or more sets of cepstral differences. The word models were talker-dependent, but the modifications were the same for all words and all talkers.

- (a) *Single Model Compensation*:— The set of cepstral mean differences and variance ratios observed in multistyle-trained models [represented by filled squares in Figure 3(a) and (c)] was applied as compensation in recognition tests on all styles.
- (b) *Multimodel Compensation*:— Three sets of cepstral mean compensations corresponding to the soft, the loud, and the shout-trained models, as well as cepstral variance ratios for multistyle-trained models, were applied to generate three new word models; together with the original normally trained word model, they were used in recognition tests on all styles. In recognition, the four models were used for each vocabulary word, and were treated independently and equally; in effect, the computation for HMM recognition was quadrupled.

The recognition error rates of these experiments are listed in Table IV along with the error rates of the baseline system and the multistyle-trained system for comparison. The error rate reductions relative to the baseline system seem quite promising given the simplicity of the compensation technique.

It is not clear how many different styles it would be useful to add in similar experiments before recognition performance would start to decline. However, evidence recently gathered<sup>23</sup> indicates that a small number of well-selected styles might be sufficient. The next section discusses a variation of the above technique — hypothesis-driven stress compensation.

<p style="text-align: center;"><b>TABLE IV</b>  <b>Substitution Rate (Percent):</b>  <b>A Comparison of Fixed Stress Compensation</b></p>								
Condition	Norm	Fast	Loud	Noise	Soft	Shout	Avg5	Avg6
Baseline HMM	1.0	6.1	29.1	19.6	13.5	86.4	13.9	25.9
Multistyle	0.5	5.6	5.1	2.1	5.8	43.6	3.8	10.5
Single Model	1.2	4.6	15.2	12.2	15.4	79.5	9.7	21.4
Multimodel	1.0	4.2	12.1	6.7	5.5	68.7	5.9	16.4

## 6. CEPSTRAL DOMAIN STRESS COMPENSATION — A HYPOTHESIS-DRIVEN APPROACH

It is the high cost of increased computation and the uncertainty about training-style sufficiency and efficiency that prompted us to search for alternatives. As a result of this effort, the hypothesis-driven cepstral mean compensation technique, which adapts to the input speech and to the hypothesized reference word, was developed. Fixed multistyle variance compensation has been found beneficial for all styles and will be used in conjunction with the adaptive mean compensation, unless stated otherwise.

As depicted in Figure 4, a talker is modeled as an information source that puts out a sequence of deterministic cepstral vectors  $\{c_t\}$ .<sup>\*</sup> Before the vectors are received by the decoder, we assume that they undergo two stages of contamination.

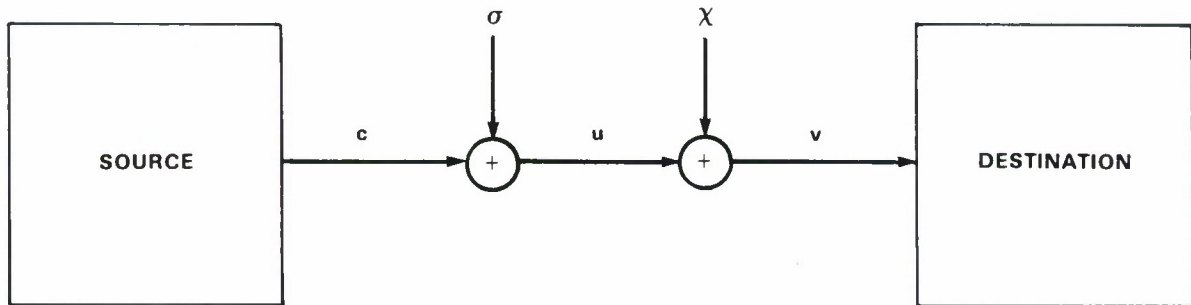


Figure 4. Model of the contamination of cepstral coefficients, where  $\sigma$  is a random noise factor and  $\chi$  is a deterministic, but unknown, stress factor.

<sup>\*</sup> The subscript  $t$  is an index of time.

### Stage 1

A sequence of independent identically distributed (i.i.d.) random vectors  $\{\delta_t\}$  is added to the cepstral sequence  $\{c_t\}$  to create a new sequence  $\{u_t\}$ :

$$u_t = c_t + \delta_t \quad . \quad (4)$$

The sequence  $\{\delta_t\}$  models the randomness of speech cepstral parameter outputs; its elements are assumed to be normally distributed with zero mean vector and diagonal covariance matrix (see discussion in Section 3).

### Stage 2

A deterministic but unknown vector  $\chi$  is added to the sequence  $\{u_t\}$  to create the observation sequence  $\{v_t\}$ , i.e.,

$$v_t = u_t + \chi \quad . \quad (5)$$

The vector  $\chi$  is the additive “stress” component. It is assumed to have the functional form [see Figure 3(a)]:

$$\chi_i = a e^{-b(i-1)} \quad , \quad (6)$$

and is further assumed to remain unchanged within a word interval.

Given a sequence of observations  $v_t$ ,  $t = 1, 2, \dots, T$  we have developed a procedure for estimation, based on maximum likelihood principles, of the parameters  $a$  and  $b$  in Equation (6). The remaining part of this section deals with the derivation of this estimation procedure; readers who are only interested in the experimental results may skip to the next section without loss of continuity.

Our parameter estimation procedure is divided into two steps, the estimation of  $\chi_i$  and the smoothing:

#### Step 1 (Estimating $\chi_i$ )

The probability density function of the observation  $v_i$  is given by

$$f(v_i) = \frac{1}{\sqrt{2\pi}\sigma_i} \exp\left[-\frac{(v_i - c_i - \chi_i)^2}{2\sigma_i^2}\right] \quad . \quad (7)$$

The likelihood function of the  $i^{\text{th}}$  observation variable,  $v_{it}$  for  $t = 1, \dots, T$ , conditioned on both the sequence of the  $i^{\text{th}}$  cepstral coefficient  $c_{it}$ ,  $t = 1, \dots, T$  and the  $i^{\text{th}}$  “stress” component  $\chi_i$  is given by

$$l(v_{i1}, \dots, v_{iT} | c_{i1}, \dots, c_{iT}, \chi_i) = \prod_{t=1}^T \frac{1}{\sqrt{2\pi}\sigma_i} \exp\left[-\frac{(v_{it} - c_{it} - \chi_i)^2}{2\sigma_i^2}\right] \quad . \quad (8)$$



Taking logarithms of both sides, we obtain the log likelihood function

$$L(v_{i1}, \dots, v_{iT} | c_{i1}, \dots, c_{iT}, \chi_i) = -T \log \sqrt{2\pi\sigma_i} - \sum_{t=1}^T \frac{(v_{it} - c_{it} - \chi_i)^2}{2\sigma_i^2} \quad (9)$$

The  $\bar{\chi}_i$  that maximize Equation (9) is the classical maximum likelihood estimate of  $\chi_i$ , it is given by

$$\begin{aligned} \bar{\chi}_i &= \frac{1}{T} \sum_{t=1}^T (v_{it} - c_{it}) \\ &= \frac{1}{T} \sum_{t=1}^T v_{it} - \frac{1}{T} \sum_{t=1}^T c_{it} \end{aligned} \quad (10)$$

We replace the sample average of  $c_i$ , which is not observable, by the expected average value, derived from the word hypothesis:

$$\begin{aligned} \bar{c}_i &= E \left[ \frac{\sum_i \tau_i c_i}{\sum_j \tau_j} \right] \\ &= \sum_i E \left[ \frac{\tau_i}{\sum_j \tau_j} \right] c_i \end{aligned} \quad (11)$$

where the  $\tau_i$ 's are a set of mutually independent discrete random variables whose values represent the dwell time in each of the  $i$  nodes, and the summations are over all speech nodes.

In Equation (11),  $\tau_i$  is known to have geometric probability mass function

$$P_{\tau_i}(k) = p_i(1 - p_i)^{k-1} \quad , \quad k = 1, 2, \dots, \quad (12)$$

where  $1 - p_i$  is the self-looping probability of node  $i$ . If the Hidden Markov Model has  $N$  speech nodes and we let the random variable  $\gamma = \sum_{i=1}^N \tau_i$ , it can be shown that if  $P_1 \neq P_2 \neq \dots \neq P_N$  the probability mass function of  $\gamma$  is the mixture distribution

$$P_\gamma(k) = \sum_{i=1}^N w_i P_{\tau_i}(k) \quad , \quad k = N, N + 1, \dots, \quad (13)$$

where

$$w_i = \prod_{\substack{j=1 \\ j \neq i}}^N \frac{p_j(1-p_i)}{p_j - p_i} \quad . \quad (14)$$

Since a closed form formula for  $E \left[ \frac{\tau_i}{\sum \tau_j} \right]$  has not been found, we use an approximation using up to the second-order moments. Let

$$\gamma_i = \sum_{\substack{j=1 \\ j \neq i}}^N \tau_j \quad , \quad (15)$$

$$g(\tau_i, \gamma_i) = \frac{\tau_i}{\tau_i + \gamma_i} \quad , \quad (16)$$

then  $\tau_i$  and  $\gamma_i$  are independent and the expectation can be approximated by

$$\begin{aligned} E[g(\tau_i, \gamma_i)] &\approx g(\bar{\tau}_i, \bar{\gamma}_i) + \frac{1}{2} \left( \sigma_{\tau_i}^2 \frac{\partial^2 g}{\partial \tau_i^2} + \sigma_{\gamma_i}^2 \frac{\partial^2 g}{\partial \gamma_i^2} \right) \\ &= \frac{\bar{\tau}_i}{\bar{\tau}_i + \bar{\gamma}_i} + \frac{\bar{\tau}_i \sigma_{\gamma_i}^2 - \bar{\gamma}_i \sigma_{\tau_i}^2}{(\bar{\tau}_i + \bar{\gamma}_i)^3} \quad , \end{aligned} \quad (17)$$

with the means and variances given by

$$\left\{ \begin{array}{l} \bar{\tau}_i = \frac{1}{p_i} \quad , \\ \bar{\gamma}_i = \sum_{\substack{j=1 \\ j \neq i}}^N \frac{1}{p_j} \quad , \\ \sigma_{\tau_i}^2 = \frac{(1-p_i)}{p_i^2} \quad , \\ \sigma_{\gamma_i}^2 = \sum_{\substack{j=1 \\ j \neq i}}^N \frac{(1-p_j)}{p_j^2} \quad . \end{array} \right. \quad (18)$$

The estimation formula (10) becomes

$$\bar{\chi}_i = \frac{1}{T} \sum_{t=1}^T v_{it} - \sum_{i=1}^N E[g(\tau_i, \gamma_i)] c_i \quad . \quad (19)$$

In Equation (19) the first sum is over the observed cepstral coefficient sequence, and the second sum is over the parameters of the hypothesized model. Therefore, we refer to this technique as a hypothesis-driven technique.

### Step 2 (Smoothing $\chi_i$ )

After  $\chi_1, \dots, \chi_{12}$  are estimated, we fit Equation (6) to them. A least-mean-square fit requires solving the following equations:

$$a = \frac{\sum \chi_i e^{-b(i-1)}}{\sum e^{-2b(i-1)}} \quad (20a)$$

and

$$\frac{\sum \chi_i e^{-b(i-1)}}{\sum e^{-2b(i-1)}} = \frac{\sum i \chi_i e^{-b(i-1)}}{\sum i e^{-2b(i-1)}} \quad , \quad (20b)$$

where Equation (20b) can be solved numerically. A less computationally intensive and yet more robust fit (i.e., one which is less susceptible to the effect of outlying data) is given by fitting exponential functions to all pairs  $\{\chi_i, \chi_j\}$ ,  $i \neq j$ , or a subset of these pairs, and then by averaging magnitudes and time constants of the fits. We have chosen to fit the pairs that contain  $\chi_1$  and one of  $\chi_2, \chi_3, \chi_4$  and  $\chi_5$ , namely,  $\{\chi_1, \chi_j\}$ ,  $j = 2, 3, 4, 5$ . Therefore,

$$b_j = \begin{cases} -\ln \frac{\chi_j}{\chi_1} & , \quad \chi_1 \chi_j > 0 \quad \text{and} \quad |\chi_1| > |\chi_j| \\ 0 & , \quad \text{otherwise} \end{cases} \quad .$$

$$a_j = \begin{cases} \chi_1 & , \quad b \neq 0 \\ 0 & , \quad \text{otherwise} \end{cases} \quad (21)$$

and  $a$  and  $b$  are the average of nonzero  $a_j$ 's and  $b_j$ 's.



## 7. SUMMARY OF THE PROCEDURE FOR CEPSTRAL COMPENSATION\* AND THE EXPERIMENTAL RESULTS

Given the cepstral vectors of a test token and the Hidden Markov word model for a reference (the procedure is done for every reference word), the procedure for the adaptive cepstral compensation and recognition is described as follows:

- Step 1:** Compute a set of stress components [c.f. Equation (19)].
- Step 2:** Smooth the stress components by fitting an exponential function to them [c.f. Equations (6) and (21)].
- Step 3:** Subtract the values of the exponential function from the cepstral vectors of the test token.
- Step 4:** In recognition, perform likelihood tests using the compensated test tokens.

In Table V we summarize the recognition error rates when the hypothesis-driven stress compensation is applied to the "simulated stress" data base. For comparison the error rates of the

<p style="text-align: center;"><b>TABLE V</b></p> <p style="text-align: center;"><b>Substitution Rate (Percent):</b></p> <p style="text-align: center;"><b>A Comparison of Multimodel Fixed Stress Compensation</b></p> <p style="text-align: center;"><b>with Hypothesis-Driven Stress Compensation</b></p>								
Condition	Norm	Fast	Loud	Noise	Soft	Shout	Avg5	Avg6
Baseline HMM	1.0	6.1	29.1	19.6	13.5	86.4	13.9	25.9
Multimodel	1.0	4.2	12.1	6.7	5.5	68.7	5.9	16.4
Hypothesis-Driven	0.9	4.7	12.7	7.0	5.7	72.4	6.2	17.2

baseline and of multimodel compensation are also included. This technique has also been applied to a more advanced 14-node, fixed-variance HMM system<sup>16</sup> whose parameters contain cepstral coefficients as well as differential cepstral coefficients. Because cepstral variances are fixed in this recognizer, no variance scaling is performed. The recognition results, with and without cepstral compensations, are listed in Table VI.

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\* The compensation technique is not restricted to a HMM baseline system, similar estimation formula can be derived for DTW (dynamic time warping) based recognition systems.

<p style="text-align: center;"><b>TABLE VI</b></p> <p style="text-align: center;"><b>Substitution Rate (Percent):</b></p> <p style="text-align: center;"><b>An Advanced HMM Recognizer</b></p>								
Condition	Norm	Fast	Loud	Noise	Soft	Shout	Avg5	Avg6
Without Compensation	0.4	1.7	3.4	2.9	4.4	49.8	2.5	10.4
With Compensation	0.4	1.7	3.4	1.4	2.4	45.3	1.9	9.0

## 8. CONFIDENCE INTERVAL ANALYSIS OF EXPERIMENTAL RESULTS

We wish to demonstrate that the reductions achieved in substitution rate are statistically significant.

Suppose that the probability of a substitution error is  $p$ ; then the probability of committing  $k$  errors in a test data base of  $n$  tokens is given by the binomial function

$$\Pr(k \text{ errors in } n \text{ tokens}) = \binom{n}{k} p^k (1-p)^{n-k} \quad (22)$$

The mean and variance of the number of errors,  $k$ , are given by

$$\begin{aligned} \mu &= np \\ \sigma^2 &= np(1-p) \end{aligned} \quad (23)$$

For large  $n$  we approximate the binomial function by the Gaussian probability density  $N[n\mu, np(1-p)]$ . The confidence interval of 95% is given by  $(\mu - 1.96 \sigma, \mu + 1.96 \sigma)$ . We define the parameter  $X$  as the ratio:

$$X = \frac{1.96 \sigma}{\mu} \quad (24)$$

so that the 95% confidence interval becomes  $(\mu - X\mu, \mu + X\mu)$ . Substituting (23) into (24), assuming  $p \ll 1$ ,

$$X \approx \frac{1.96}{\sqrt{np}} = \frac{1.96}{\sqrt{\mu}} \quad (25)$$

For  $n = 8400$ ,  $p = 13.9\%$  (5-avg, baseline HMM) and  $p = 2.5\%$  (5-avg, advanced HMM), we have  $X = 5.7\%$  and  $X = 13.5\%$ , respectively. The 95% confidence intervals, corresponding to  $p = 13.9\%$  and  $p = 2.5\%$ , are roughly (13.1%, 14.7%) and (2.16%, 2.84%), respectively. In Table V, the substitution error rate  $p = 6.2\%$  (5-avg, hypothesis-driven compensation) lies well outside the interval (13.1%, 14.7%); similarly in Table VI the error rate  $p = 1.9\%$  (5-avg, compensation) lies well outside the interval (2.16%, 2.84%). Hence the improvements obtained using this type of compensation are statistically significant.

## 9. CONCLUSION

Spectral tilt has been found to vary significantly for speech spoken in stressful talking environments. We studied the statistical variations of cepstral coefficients embedded in the framework of Markov models and found that the observed changes in cepstral mean values, from normal speech trained models to simulated-stress trained models, corresponded approximately to an exponential type of spectral tilt. A simple and efficient compensation technique, the hypothesis-driven cepstral compensation, has been formulated. Using this simple compensation technique, recognition experiments yielded significant reduction in error rate.

It is likely that further improvement may be achieved via reliable silence/voiced/unvoiced separation before the application of cepstral coefficient compensation, with compensation for spectral tilt only in voiced segments. A Bayes estimate, that incorporates and updates *a priori* knowledge of the distributions of the stress component  $\chi_i$  and of the parameters  $a$  and  $b$  in the smoothing process, may also be superior to our estimate. Other improvements may be achieved through more detailed understanding and modeling of speech variations in stress.

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## APPENDIX

### LIST OF WORDS IN THE “SIMULATED STRESS” VOCABULARY

zero	airspeed	east	mode	sensor
ten	air	echo	narrow	south
one	alpha	elevation	nav	standby
twenty	altitude	negative	north	start
two	auto	erase	north	status
thirty	azimuth	fix	no	steerpoint
three	back	freeze	off	step
forty	bar	fuel	oh	stop
fifty	bravo	go	out	synthesis
five	break	ground	point	target
sixty	change	hello	profile	thousand
six	Charlie	help	quiet	threat
seventy	combat	history	radar	tracker
seven	comm	hot	range	train
eighty	confirm	hundred	recall	voice
eight	control	inventory	release	weapon
ninety	cursor	lock	repeat	west
nine	degrees	map	return	white
advise	delta	mark	rubout	wide
affirmative	destination	medium	select	yes

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